

## 11.4 - Combined Gas Law - Putting it all together!

Minds On! RECAP

Fill in the blanks:

STP: \_\_\_\_\_ P = \_\_\_\_\_ T = \_\_\_\_\_

SATP: \_\_\_\_\_ P = \_\_\_\_\_ T = \_\_\_\_\_

Boyle's Law: \_\_\_\_\_

Charles's Law: \_\_\_\_\_

Gay-Lusac's Law: \_\_\_\_\_

Do you think this is realistic? That only TWO variables change at a time → NO!

Combined Gas Law:

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

Practice Rearranging for:

 $V_2 =$ 

$$T_2 = \frac{P_2 \cdot V_2 \cdot T_1}{P_1 \cdot V_1}$$

**Example 1:**

Alex is having a birthday party on a mild winter's day. The weather changes and a higher-pressure (103.0 kPa) cold front (-25°C) rushes into town. The original air temperature was -2°C and the pressure was 100.8 kPa. What will happen to the volume of the 4.2 L balloons that were tied to the front of the house?

$$\begin{aligned}
 P_1 &= 100.8 \text{ kPa} & P_2 &= 103.0 \text{ kPa} & V_2 &= \frac{P_1 \cdot V_1 \cdot T_2}{T_1 \cdot P_2} \\
 V_1 &= 4.2 \text{ L} & V_2 &= ??? & & \\
 T_1 &= 271 \text{ K} & T_2 &= 248 \text{ K} & & \\
 & & & & & = \frac{100.8 \cdot 4.2 \cdot 248}{271 \cdot 103.0} \\
 & & & & & = 3.76 \text{ L} \\
 & & & & & = \boxed{3.8 \text{ L}} \quad \downarrow V \text{ as } \uparrow P \text{ \& } \downarrow T
 \end{aligned}$$

**Example 2:**

An automated instrument has been developed to help drug-research chemists determine the amount of nitrogen in a compound. Any compound containing carbon, nitrogen and hydrogen is reacted with copper (II) oxide to produce CO<sub>2</sub>, H<sub>2</sub>O and N<sub>2</sub> gases. The gases are collected separately and analyzed.

In an analysis of 39.8 mg of caffeine using this instrument, 10.1 mL of N<sub>2</sub> gas was produced at 23°C and 746 torr. What must the new temperature of nitrogen be, in °C, if the volume is increased to 12.0 mL, and the pressure is increased to 780 torr?

$$\begin{aligned}
 P_1 &= 746 & P_2 &= 780 \text{ torr} & T_2 &= \frac{P_2 \cdot V_2 \cdot T_1}{P_1 \cdot V_1} \\
 V_1 &= 10.1 \text{ mL} & V_2 &= 12.0 \text{ mL} & & \\
 T_1 &= 296 \text{ K} & T_2 &= ?? & & \\
 & & & & & = \frac{780 \cdot 12.0 \cdot 296}{746 \cdot 10.1} \\
 & & & & & = 368 \text{ K} - 273 \text{ K} \\
 & & & & & = 94.7^\circ \text{C} \\
 & & & & & = \boxed{95^\circ \text{C}}
 \end{aligned}$$

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

## Practice Problems

1. A sample of gas has a volume of 150 mL at 260K and 92.3 kPa. What will the new volume be at 376K and 123 kPa?

$$\begin{aligned}
 P_1 &= 92.3 \text{ kPa} & P_2 &= 123 \text{ kPa} & V_2 &= \frac{P_1 \cdot V_1 \cdot T_2}{T_1 \cdot P_2} \\
 V_1 &= 150 \text{ mL} & V_2 &= & &= \frac{92.3 \cdot 150 \cdot 376}{260 \cdot 123} \\
 T_1 &= 260 \text{ K} & T_2 &= 376 \text{ K} & &= 163 \text{ mL}
 \end{aligned}$$

2. A cylinder at 48 atm pressure and 290 K releases 35 mL of carbon dioxide gas into a 4.0 L container at 297 K. What is the pressure inside the container?

$$\begin{aligned}
 P_1 &= 48 \text{ atm} & P_2 &= ? \\
 V_1 &= 35 \text{ mL} & V_2 &= 4,000 \text{ mL} \\
 T_1 &= 290 \text{ K} & T_2 &= 297 \text{ K} \\
 P_2 &= \frac{P_1 \cdot V_1 \cdot T_2}{T_1 \cdot V_2} \\
 &= \frac{48 \cdot 35 \cdot 297}{290 \cdot 4,000} \\
 P_2 &= 0.43 \text{ atm}
 \end{aligned}$$

3. In a large syringe, 48 mL of ammonia gas at STP is compressed to 24 mL and 110 kPa. What must the new temperature of the gas be?

$$\begin{aligned}
 P_1 &= 101.325 \text{ kPa} & P_2 &= 110 \text{ kPa} & T_2 &= \frac{T_1 \cdot P_2 \cdot V_2}{P_1 \cdot V_1} \\
 V_1 &= 48 \text{ mL} & V_2 &= 24 \text{ mL} & &= \frac{273 \cdot 110 \cdot 24}{101.325 \cdot 48} \\
 T_1 &= 273 \text{ K} & T_2 &= ? & &= 148 \text{ K}
 \end{aligned}$$

4. A 100 W light bulb has a volume of 180.0 cm<sup>3</sup> at STP. The light bulb is turned on and the heated glass expands slightly, changing the volume of the bulb to 181.5 cm<sup>3</sup> with an internal pressure of 214.5 kPa. What is the temperature of the light bulb (in °C)?

$$\begin{aligned}
 P_1 &= 101.325 \text{ kPa} & P_2 &= 214.5 \text{ kPa} & T_2 &= \frac{T_1 \cdot P_2 \cdot V_2}{P_1 \cdot V_1} \\
 V_1 &= 180.0 \text{ cm}^3 & V_2 &= 181.5 \text{ cm}^3 & &= \frac{273 \cdot 214.5 \cdot 181.5}{101.325 \cdot 180} \\
 T_1 &= 273 \text{ K} & T_2 &= ? & &= 583 \text{ K}
 \end{aligned}$$

5. Sulphur hexafluoride, SF<sub>6(g)</sub>, is used as a chemical insulator. A 5.0 L sample of this gas is collected at 205.0°C and 250 kPa. What pressure must be applied to this gas sample to reduce its volume to 1.7 L at 25°C?

$$\begin{aligned}
 P_1 &= 250 \text{ kPa} & P_2 &= ? & P_2 &= \frac{P_1 \cdot V_1 \cdot T_2}{T_1 \cdot V_2} \\
 V_1 &= 5.0 \text{ L} & V_2 &= 1.7 \text{ L} & &= \frac{250 \cdot 5.0 \cdot 298}{478 \cdot 1.7} \\
 T_1 &= 478 \text{ K} & T_2 &= 298 \text{ K} & &= 458 \text{ kPa}
 \end{aligned}$$